

The mathematical model for regression formulas fitted to the data were linear and none linear function. These are functions of these types

Linear, $Y = mx + c$ 1

Power, $Y = mX^c$ 2

Exponential, $Y = m \ln(X) + c$ 3

Polynomial $Y = aX_n + aX_{n-1} + \dots + aX_1 + c$4

Where Y a main dimension function and

X is the bollard pull bp of the tugboats

m, c, and n are constants determined by the regression analysis.

These are well known mathematical procedures according to reference[8], and others. The Microsoft EXCEL add in software has these program for these procedures and these are used for the regression analysis in this work.

Numerous regression correlation were made between different formulated tug parametric variables and the bollard pull but only those reliable formulas with correlation coefficient R^2 greater than 0.8 are selected and published in this paper in fig 2 to fig 14. Table 2 show the summarized formulas of the regression analysis where the number of data points N and the regression coefficients R^2 are also shown.

Table 3 and 4 show an example of the Microsoft EXCEL spread-sheet method for using these formulas to calculate the main dimensions of tug boat for a particular bollard pull described below.

III. RESULT AND DISCUSSION

The resulting formulas from this work are shown in diagrams (fig 2 to 14) and table 2. If, for example, the required sustained bollard pull for a tow is calculated to be 28mt. What will be the main dimension and power of the tug for the tow? Table 3 show the formulas entered in EXCEL work-sheet as Eq(1), Eq(2) etc for the computation of each of the main dimensions. Appropriate combinations of these formulas as shown in some cases are necessary to compute a particular dimension of the projected tug boat. Table 4 show the result of dimensions of tugs that is required to carry out the towing work.

effectively with the mean expected value of $L = 28.08m$, $B = 8.58m$, $D = 3.69m$ $T = 3.14m$, and $= 2211hp$

IV. CONCLUSIONS

Bollard pull is the major important parameter in the design and operation criteria of tug boats propulsion system. This paper focuses on the determination of the dimensional parameters length L, breadth B, depth D, Draft T in meters and power P in horse power of the tug as a function of the main bollard pull bp in metric tons. The necessary formulas for carrying out this task are derived by regression analysis from data collated from 116 world existing tug boats. The thirteen formulas derived and shown have regression coefficient R^2 greater than 0.8. This formulation is very important for the prediction of the optimum main particulars of the prospective or projected tug boat needed to tow other marine equipment (ships, barges, rigs, etc) as shown in the example stated in this paper. The formulas can also be used in a computer program for the design of tug boats.

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Table 1 A collection of the principal dimension of modern Tugboat, including bollard pull bp

Table 1 A collection of the principal dimension of modern Tugboat Including bollard pull bp								
NAME	CLASS	BUILLT	LAO(m)	B(m)	D(m)	T(m)	bp(mt)	ME(hp)
140904 VW	TURKEYBV	2016	14.8	5.9	3	2.15	19	1660
140113 VW	SPAIN	2011	16	5.5	2.8	2.15	12.5	780
151118 VN	ITALY	1986	19	5.37	2.75	2.28	2	577
130718-VN	ISTBUL RINA	2011	19.95	7	3.2	2.2	15	1200
BEN FOSS		1980	23.71	8.00	3.34	2.95	26.4	1700
141057 vw	hollandBV	2012	24.07	12.97	4	3.8	53.4	3820
121063-VO	SPAIN RINA	1982	25	8.4	4.36	4.2	32	2030
160524-VW	SPAIN	1968	25.86	6.4	3.05	3	12	825
151228 VW	HOLLAND	2007	26	11.5	3.5	2.25	33	2400

	BV							
131028-vo	holland bv	2005	26.09	7.94	4.05	3.75	50.7	3500
ARI CRUZ - SINUK	USABS	1995	26.15	8.69	3.05	2.51	11.34	1248
ES TAURUSINDO	CHINA/NKK	1997	26.45	7.96	3.47	3.19	15	1240
151103VW	USABS	1982	27.43	9.75	3.41	2.59	23.5	2110
OLIKTOK			27.89	8.17	4.2	3.93	25	2100
9777-tg-om	SINGAPORE	1995	28.4	6.5	4.11	3.47	39.05	2800
8710-TG-OM	ITALI RINA	1985	28.55	6.56	3.82	3.14	8.7	1520
11326-TG-OM	SingaporeABS	2006	29	9	4.25	3.5	40	3200
11326-TG-OM	ABS		29.1	9	4.25	3.5	30	2400
11346-TG-OM	FRANCE GL	1976	29.2	8.5	4.15	3.5	30	1500
12592-TG-OM	RUSSIA	1988	29.3	8.3	4.3	3.4	16	1604
CONTELLATION	NS	2009	30.22	9	4.38	3.68	30	2400
Island Brave	USA ABS		30.99	11.00	5.59	4.60	70	5364
11077-TG-OM	BatamIn LR	2005	31	9	4.5	3.5	40	3000
11153-OT-OM	SPAIN	2002	31.21	8.41	4.51	4	22.9	1716
T W Ocean 15	USA ABS	1998	31.52	11.28	5.49	4.27	53.8	3900
140821-VO	BV	2014	31.65	9.14	4.2	3.65	40	3200
150909 VO	USA ABS	2003	31.70	10.97	4.88	4.11	48.58	4200
TITO N SETTIMO	LR	2012	31.99	11.6	5.81	5.36	73	5364
ASD TYR	USA ABS		32.00	11.58	5.94	5.36	83.45	6834
13082 TG-OM	USA ABS	1999	32.00	10.36	5.03	4.88	62.6	4400
12985 TG OM	USA ABS	2012	32.00	11.58	5.38	5.23	60.78	4720
11163-TG-OM	turkishBV		32.5	11.7	5.6	4.3	65	5632
130643-VO	CHINA ASD	2009	33	10	4.5	4.1	50	4000
141120 VO	INDONESIA	1982	33.52	7.92	3.2	2.4	12	1273
CHEV RICHMOND	CHINA	2013	33.98	10	4.5	3.4	50	4000

Table 1. Continued

NAME	CLASS	BUILT	LAO(m)	B(m)	D(m)	T(m)	bp(mt)	ME(hp)
9547TGOM		2016	34.4	12.82	5.75	5.36	70	6303
9835-TG-OM	CHina BV	2014	34.5	9.5	4.6	3.65	40	3200
5922-TG-OM	MALAY BV	2016	35	11.5	5.62	4.8	62	5150
12885-TG-OM	china BV	2014	36	10.97	5	4.1	40	3200
140413-VO	china BV	2014	36	10.97	5	4.1	40	3200
120322-VW			36.02	10.6	4.8	3.6	64	5200
ocean Tower	CHINA BV	2009	36.1	10.6	4.9	4	40	3200
ESCORT EAGLE	LAUSABS	1970	36.58	9.45	4.54	4.11	37.5	3000
11321-TG-OM	KOREA	2012	36.9	10	4.5	3.4	59.464	4500
11143 TUG OM		2007	37	10.6	4.95	4	40.85	3200
11275-TG-OM	AFRCA/IRE	1978	37.3	10.84	4.9	4.3	40.6	3500
141137-VA	LRDAMEN	1998	37.5	9.25	4.9	3.4	69	5000

SUIATTIEUS	CCS CSA CSM	2012	37.7	10.4	4.8	3.65	65	5200
AHT	LRCHINA		37.99	11.00	5.00	3.81	60	4960
Liberty	CHINA	2014	50	15.5	7.7	5.5	105	8400
HERCULES	CHINABV	2012	58.7	14.6	5.5	4.75	66	4890
ASTERI	KEPPEL	2004	60	16	6	5	78.3	6000
150336 VA	SINGAPORE	2000	60	13.8	6.8	5.6	124	8000
9397-TG-OM	GERMANY ABS	1982	64.5	13.82	6.9	5.91	110	8160
140929	US ABS	2015	66.5	16	6.5	5.12	80	6400
9397-TG-OM			26.15	7.95	4.05	3.45	38	2720
140929-VA	DAMEN	1999	26.15	7.95	4.05	3.45	38	2720
M MORAN		2012	36.6	10.5	4.6	3.3	51	4800
Robust	SINGAPORE	2013	81	16.8	7.5	6.4	120	7000
OCEAN Wrestler	SINGAPORE	2013	81	16.8	7.5	6.4	120	7000
150632	AUTR	2013	91	22	9.6	8	240	21456
STAN2608	DAMEN		26.15	7.95	4.05	3.45	38	5440

Table 2 Tugboat design formulas as a function of bollard pull(x = bp) in metric tonnes.

N	R ²	Formula	Eq. no
116	0.900	B = -2E-04x ² + 0.0912x + 5.78 -----	Eq1
83	0.898	D = -7E-05x ² + 0.046x + 2.7135 -----	Eq2
60	0.801	T = -6E-05x ² + 0.0379x + 2.2631-----	Eq3
48	0.897	P/L = 0.0002x ³ - 0.0105x ² + 1.9129x + 27.443 -----	Eq4
60	0.858	P/B = 0.0003x ³ - 0.0928x ² + 11.765x -----	Eq5
60	0.916	P/D = 0.0006x ³ - 0.2093x ² + 25.759x -----	Eq6
116	0.906	LB = 0.0102x ² + 5.4694x + 50 -----	Eq7
66	0.820	DT = 0.0005x ² + 0.4277x -----	Eq8
60	0.836	P/T = 0.0007x ³ - 0.2549x ² + 31.339x -----	Eq9
60	0.882	LBD = 0.2457x ² + 22.939x -----	Eq10D
60	0.879	LBT = 0.1953x ² + 23.382x -----	Eq10T
116	0.967	P = 0.0562x ² + 75.309x -----	Eq11
116	0.818	(√L)/ B ² = 0.3725x ^{-0.483} -----	Eq12
48	0.896	P/L = 0.0002x ³ - 0.0105x ² +1.9129x+27.443 -----	Eq13
53	0.863	bp/L= 0.0937x ^{0.7037} -----	Eq14
79	0.891	P/D = 0.0005x ³ -0.1657x ² +21.602x+93.902-----	Eq15
60	0.812	DT = 0.3367x + 4.0752 -----	Eq16
60	0.836	BT = 0.7509x + 7.8674 -----	Eq17
103	0.872	BD = 0.0006x ² + 0.6904x + 14.119 -----	Eq 18

Table 3 EXCEL layout for calculation of principal dimension of tugboat for bp = 28mt using.

	A	B	C	D	E	F
1	LOA(m)	B(m)	D(m)	T(m)	P(t)	(t)
2	bp/Eq14	Eq 1	Eq2	Eq3	Eq11	bp
3	Eq8/B2	Eq7/A3	Eq 11/EQ6	Eq11/EQ9	B2*Eq5	
4	Eq10D/(B2*C2)	Eq11/EQ5	Eq8/D3	Eq8/C2	A2*Eq4	
5	Eq10T/(B2*D2)	√([(√A2)/Eq12])	Eq10D/(A4*B4)	Eq9T/(A2*B2)	C2*Eq6	

6	Eq10T/(B3*D3)	Eq10T/(A2*D2)	Eq10D/(A2*B2)	Eq8/C1	D2*Eq9	
7	Eq10D/(B3*C3)	Eq10T/(A4*D5)	Eq10D/(A3*B3)	Eq8/C5	A3*Eq4	
8	(Eq12*(B2) ²) ²	Eq10D/(A2*C2)	Eq10D/(A8*B8)	Eq8/C6	B4*Eq5	
9	(Eq12*(B3) ²) ²	Eq10D/(A3*C3)	Eq10D/(A9*B9)	Eq10T/(A3*B3)	C3*Eq6	
10	(Eq12*(B4) ²) ²	$\sqrt{[(\sqrt{A3})/Eq12])}$	Eq10D/(A5*B5)	Eq10T/(A7*B5)	D3*Eq9	
11	(Eq12*(B5) ²) ²	$\sqrt{[(\sqrt{A4})/Eq12])}$	Eq10D/(A10*B10)	Eq10T/(A9*B9)	A4*Eq4	
12	E2/Eq13	Eq18/C2	Eq16/D2	Eq17/B2	Eq15*D3	
	FIND AVERAGE OF EACH COLUMN					

Table 4 EXCEL layout for calculation of principal dimension of tugboat for bp = 28mt using.

	A	B	C	D	E	F
1	LOA(m)	B(m)	D(m)	T(m)	P(hp)	bp(mt)
2	29.318	8.255	3.947	3.277	2152.713	28
3	25.577	8.255	2.955	3.106	2173.185	28
4	25.627	8.177	3.729	2.935	2262.252	28
5	29.859	8.525	3.984	3.338	2250.827	28
6	31.502	8.407	3.450	2.935	2271.196	28
7	34.229	9.472	3.954	2.907	1973.557	28
8	25.776	7.216	4.489	3.358	2173.185	28
9	24.818	11.048	3.045	3.826	2152.713	28
10	24.818	8.239	3.280	2.768	2751.309	28
11	29.318	8.243	4.083	2.946	1977.471	28
12	27.898	8.594	4.120	3.500	1.800.620	28
	27.945	8.594	3.730	3.174	2171.556	= MEAN

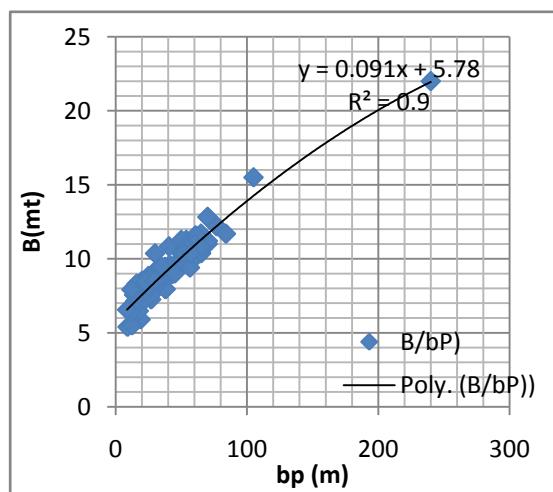


Fig 2. Breadth B of Tug boat correlation with bollard pull bp.

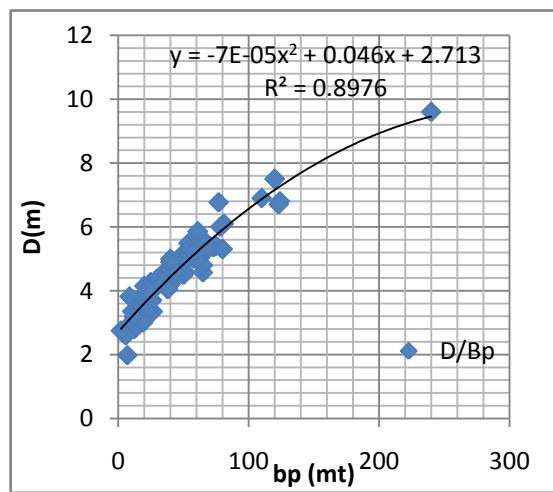


Fig 3. Depth D of Tug boat correlation with bollard pull bp

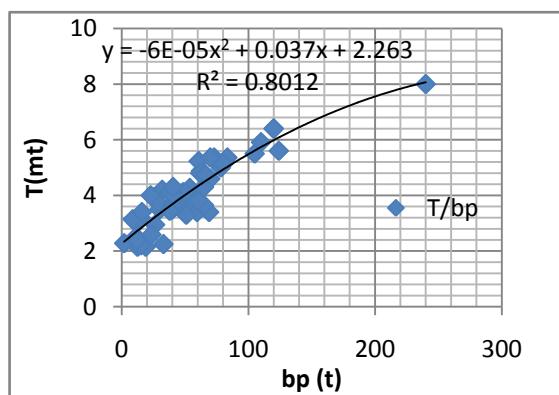


Fig 4. Draft T of Tug boat correlation with bollard pull bp.

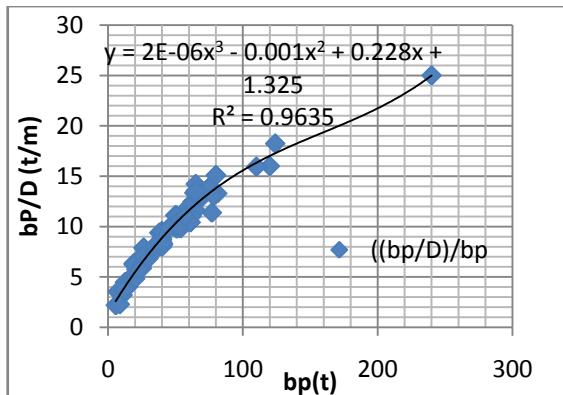


Fig 5. bp/L of Tug boat correlation with bollard pull bp

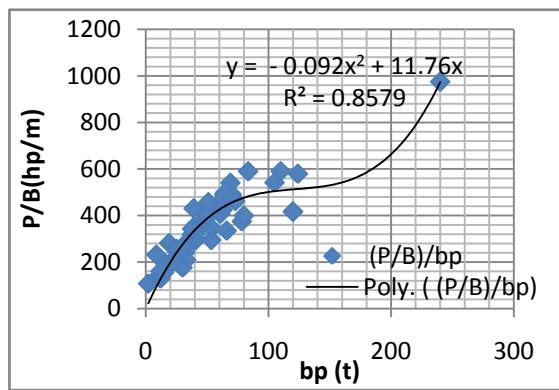


Fig 6. Power P/Breadth B ratio of Tug boat correlation with bollard pull bp.

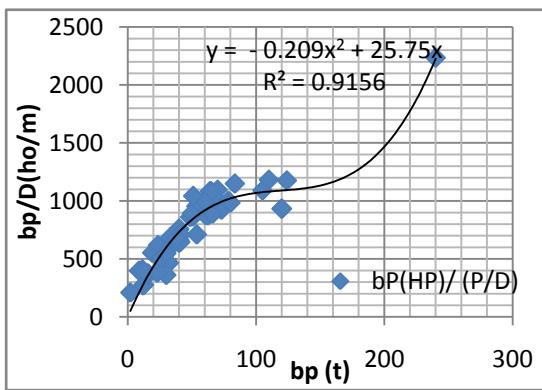


Fig 7. Power P/ Depth D ratio of Tug boat boat correlation with bollard pull bp

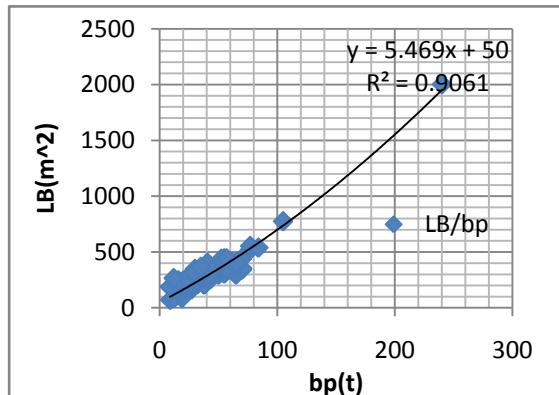


Fig 8. Length L* breadth B of Tug boat correlation with bollard pull bp

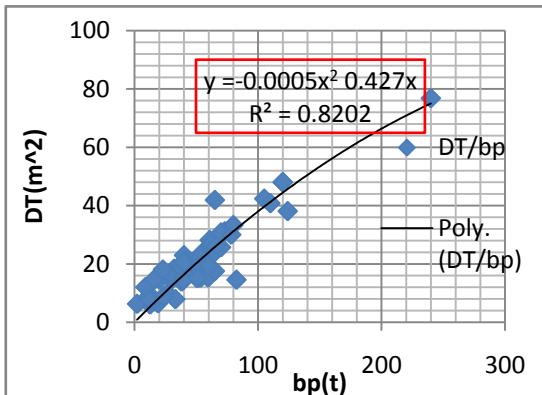


Fig 9. Depth D* draft T of Tug boat correlation with bollard pull bp

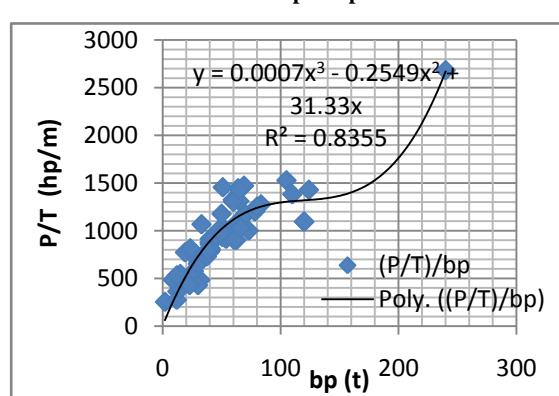


Fig 10. Power P/Draft T ratio of Tug boat correlation with bollard pull bp

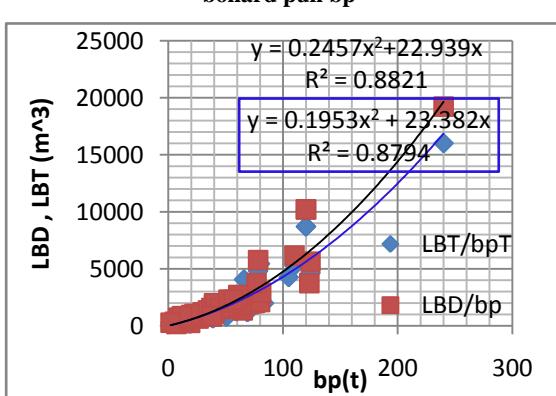


Fig 11. LBD, and LBT cubic numbers of tug boat correlation with bp

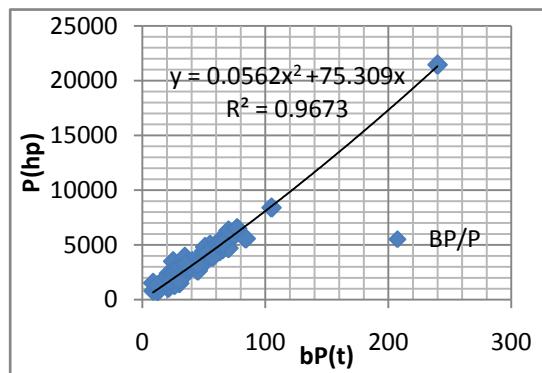


Fig 12. Power P of Tug boat correlation with bollard pull bp.

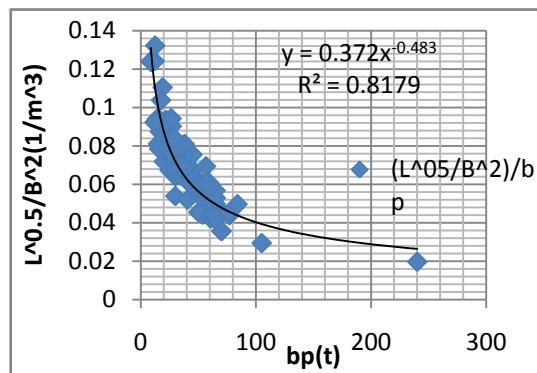


Fig 13. $(\sqrt{L})/B^2$ ratio of Tug boat correlation with bollard pull bp

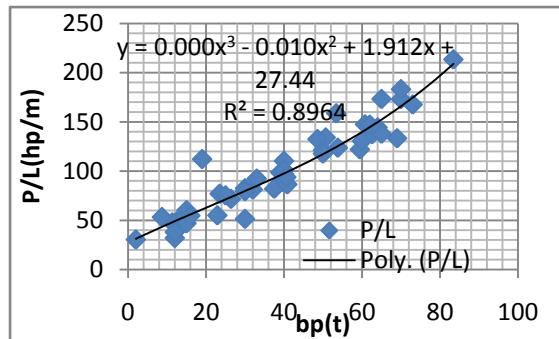


Fig 14. Power P/ Length L ratio of Tug boat Correlated with bollard pull bp

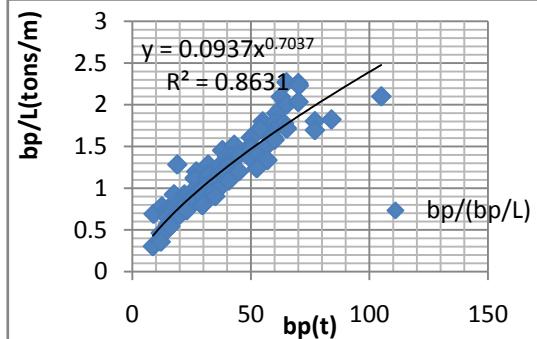


Fig 15 bp/L correlation with bollard correlated with bollard pull bp

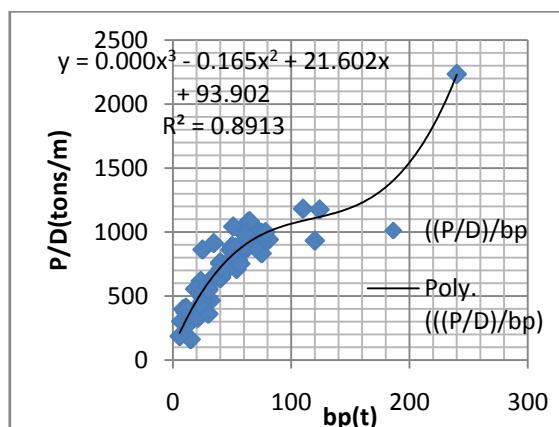


Fig 16. Power P/ Depth d ratio of Tug boat Correlated with bollard pull bp

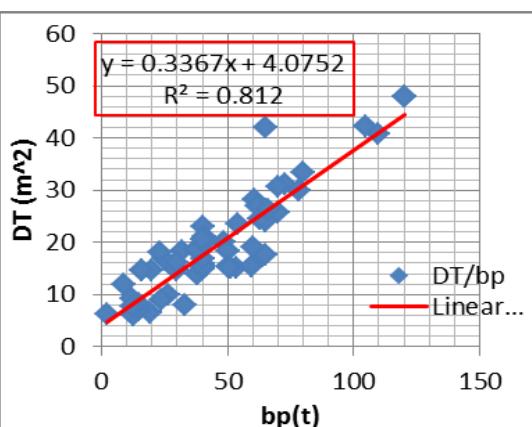


Fig 17 bp/L correlation with bollard correlated with bollard pull bp

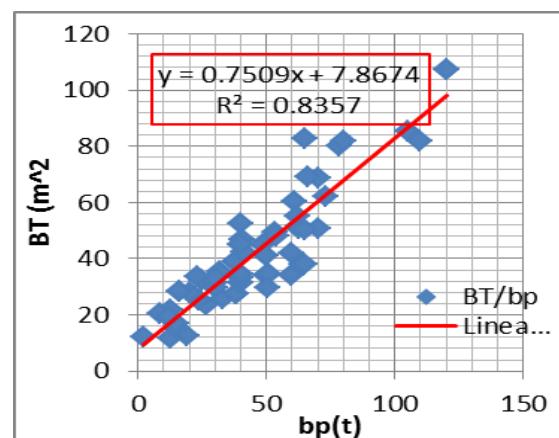


Fig 18. Power P/ Length L ratio of Tug boat Correlated with bollard pull bp

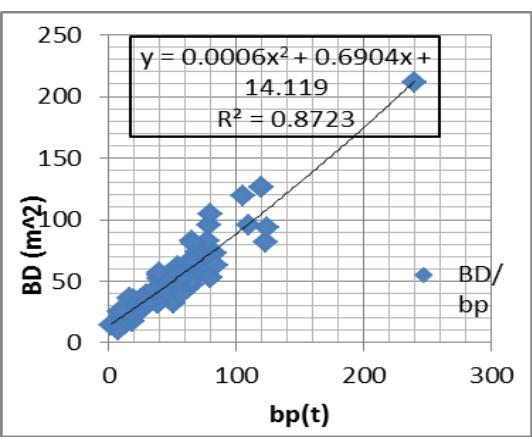


Fig 19 bp/L correlation with bollard correlated with bollard pull bp