

Original Article

# Weighed Quadratic Wolf Optimization Techniques to Enhance the Reliability and Accuracy on Beam Forming

Y. Sahithi<sup>1</sup>, P. Siddaiah<sup>2</sup>

<sup>1,2</sup>Electronics and communications Engineering, Acharya Nagarjuna University, Andhra Pradesh, India

<sup>1</sup>yarlagaddasahithi@gmail.com

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**Abstract** - Significant efforts have been made to develop an automated system to improve the antenna array beam forming. The Diagonal Loading (DL) technique is popular in determining the necessary factor loadings. Instead of constant diagonally loaded or Adhoc ways, a variable loading approach using Weighed Quadratic Wolf Optimization (WQWO) is used to achieve optimum results. The suggested technique is unique since it does not necessitate a complicated data strategy to determine the necessary loads. To address the problems, we suggest data-dependent reloading. The loaded component may be calculated entirely from the array of data provided. Analytic formulae for assessing the suggested product's performance in unpredictable guiding vector inaccuracy are indeed developed. The proposed WQWO technique enhances the reliability demonstrated by using experimental findings compared to previous DL techniques.

**Keywords** - Beamforming, Diagonal loading, Weighed Quadratic Wolf Optimization.

## 1. Introduction

For centuries, arrays of the digital signal have indeed been explored as a promising approach for information identification and an estimate in challenging environments. This ensemble of detectors may be built in various ways to leverage signals and noisy spatial properties, but it offers several benefits over a detector [1]. Steady and adjustable array beam formers are the 2 types of matrix beam formers. The constant beam former's mass is usually pre-determined but does not fluctuate depending on the program [2]. This adjustable beam former modifies its load autonomously based on conditions. This substantially outperforms the fixed beam former in terms of noise and interfering reduction. The Linearly Constrained Minimum Variance (LCMV) beamformer is a good example [3].

While there are collection defects, including guiding directions fault, lag time errors, phasing faults of the arrays' sensor, multi-path propagating influences, and wavefront aberrations, these adaptable beam formers' effectiveness suffers greatly [4]. The problem can be defined as targeted signal suppression. Numerous restrictions were proposed in adaptable arrays to solve the issue of guiding directional inaccuracy [5]. This method's concept is self-evident. The microarray processing develops resilience in the location wherein restrictions are placed; they are applied in various directions in the neighborhood of the presumed ones [6]. Nevertheless, the number of restrictions accessible is limited due to the limitations are using the matrix computer's Degrees of Freedom (DOFs) during interference cancellation [7].

A new method emerges when derivatives restrictions are added to the arrays computer. The array's performance is virtually smooth inside the region of the desired orientation when derivatives restrictions are applied. Inside the intended orientation, this beam former does have a broad focal length [8]. That beam former doesn't cancel the destination signal, even if the guiding directional mistake is minor. Nevertheless, because extra derivatives restrictions utilize the beam former's DOFs, the broad bandwidth comes at the price of lower interfering reduction capabilities [9]. With blocked matrices architecture, derivatives restrictions could be utilized to produce neither a uniform reply of the array processors nor a uniform blank inside the orientation of the anticipated signal. Throughout changes in factors, including guidance mistakes, phasing faults or array geometrical errors, polynomial restrictions could be utilized to minimize the normalized average squared divergence between required array answers and the processing answer [10-12].

## 2. Materials and methods

Each array computes intrinsic defects, including geometrical inaccuracy, reaction mistakes etc., which can be eliminated using calibration-based methods. Nevertheless, it cannot remove dynamic mistakes like guiding mistakes whenever the origin travels in a position close to the supposed orientation [13]. This look direction is guided to the continually predicted Direction-of-Arrival (DOA) in focus monitoring systems. Another issue would be that, inside the presence of the desired signal, such a technique



could mistrack towards the disturbance, provided additional techniques are developed to narrow the monitoring zone [14]. Regarding application areas, a resilient beam former continuously looks for the best orientation [15]. Concerning directing orientation errors, it maximizes the average energy output of the Capon beam former using 1<sup>st</sup>-order Taylor series approximations. In terms of intervention reduction, that technique doesn't benefit from performance degradation [16].

Since there are many faults, including driving directional mistakes, array's geometrical mistakes, and arrays sensors phasing mistakes, overall performance deteriorates. Only the driving orientation is considered a vector combination of the collection steering vector. The presumed paradigm of an Arrays Steered Vectors (ASV) is broken whenever numerous flaws occur. Subsequently, effective techniques have made advantage of an ASV's uncertainties collection. This actual ASV is considered an ellipse with the apparent ASV at its center. Inside an expected ambiguity setting, these proposed beam formers are resistant to random variations in real ASV. Those beam formers are all the same and use diagonal solutions [17]. The restriction method may be used to determine the diagonal rating.

Both utilization of observational data and an informational message regarding origin DOA are balanced in an adjustable beam former that used a Bayesian method. DOA is considered a discrete random variable with a differential Probability Distribution Function (PDF) that describes the ambiguity regarding source DOA throughout this method [18]. An assessment approach of Weighed Quadratic Wolf Optimization (WQWO) beam formers yields the final beam former. It is aimed at a collection of potential DOAs, with the percentage impact of every WQWO beam former calculated from the DOA's posterior PDF conditional on observational data. A simple estimate to the posterior PDF gives a simple construction that is more difficult than the LCMV beam former but significantly less complicated with data-driven beam formers. The Bayesian beam former outperforms the LCMV and the data-driven beam formers in several circumstances.

This resilient WQWO beam former with a single WC requirement developed to use an incremental gradients reduction method with an ad - hoc basis approach will be the first of two effective ad hoc solutions to the WC efficiency optimization problem. Rather than using a Newton-like technique, it calculates the Lagrange multiplier. This technique has several advantages, including flexibility, minimal computing burden, and the absence of sample-matrix inverted or Eigen reduction. A geometrical understanding of the execution has already been given to support the theoretical aspects. Using a new multiple WC requirements approach, a durable continuous LCMV beam former with Many Beams WC (MBWC) restrictions is

created. The Lagrange approach is used to tackle this optimization issue, revealing that calculating a series of nonlinear equations is required to solve the resilient LCMV beam former under MBWC limitations [19]. As a result, solving the resulting system of nonlinear solutions, which generates a vector of Lagrange multipliers, requires a Newton-like technique. It is worth mentioning that even these methods use ad - hoc basis strategies to maximize beam former voltage output whilst keeping the guiding direction cylindrical. Nevertheless, at low signal to noise, the adaptable beam former is susceptible to noise amplification, necessitating the use of an extra restriction to carry the elliptic limitation [20].

### 3. System Model

Adaptive beam forming correlation analysis, which will be utilized to create the beam former weighted sum, is determined using a priori information of actual demographics of the collected data in optimal beamformer. Adaptive beamforming is a methodology that provides a network of antennae to maximize receptions in a certain location by predicting the information entering from that location while rejecting signals with the same frequencies from other locations. It is accomplished by changing the weighting of each of the element's detectors. Even though the information from separate emitters is broadcast on the same frequency component, they come from various directions. The optimal weighting is generated repeatedly using sophisticated techniques that rely on many parameters in adaptive beamforming. To acquire the best panel weighting for an adjustable beam former, the autocorrelation or association matrices must always be calculated from uncertain characteristics of array images.

Whenever fewer over p+1 details are collected, the variance p-dimensional matrices estimation turns singular and thus useless. It is a poor approximation of the real correlation matrix until more than p+1 samples are provided. Varied techniques for estimating the covariance matrix might result in multiple attitudes and commitments to the program. The ensembles mean of Rx, and  $M * M$  matrices, is estimated using blocks of pictures in the blocking adaptable Sample Matrix Inversion approach, which is expressed as:

$$S_a = F\{x(i)a^G(i)\} = \frac{1}{N} \sum_{i=1}^I z(i)a^G(i) \tag{1}$$

$$N\sigma_r x_0 x_0^G + S_k + S_m \tag{2}$$

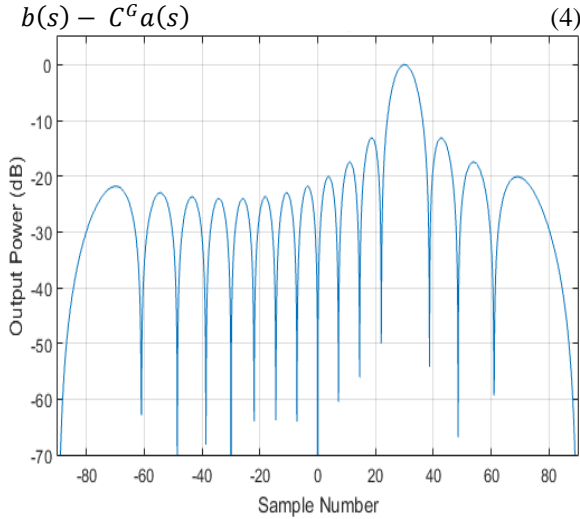
$\sigma_r$  is the strength of the received signals,  $i$ ,  $S_k$  represents jammer and  $S_m$  noise similarity matrices in both.

Where N is the number of screenshots being used,  $i$  is the number of systems

$$S_{i+m} = S_i + S_m \tag{3}$$

**3.1. Conventional Beamformer**

The output signal is given by:



**Fig. 1 The beam pattern using traditional beam shaping**

Beam's former Maximization result is as follows:

$$Q = \sum_c^{Maximum} \{ |b|^2 \} = [C^G a(s)]_c^{Maximum} \quad (5)$$

Solving this equation gives

$$c = \frac{x_0}{\sqrt{x_0^G x_0}} \quad (6)$$

$x_0$  is the steering vector.

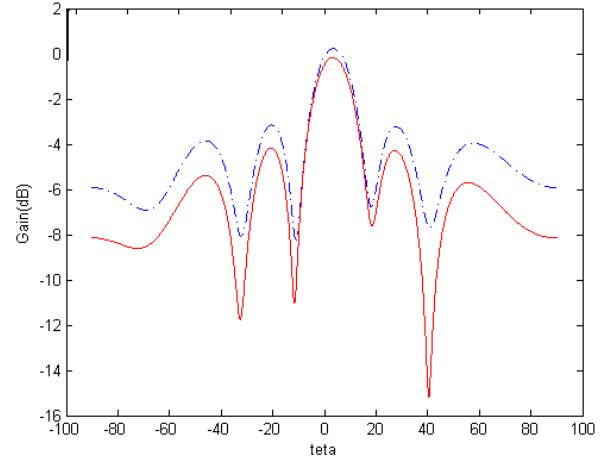
**3.2. WQWO Beamforming**

This restriction 'g' might be read as gain in the gaze direction that must be kept constant. An LCMV deviation beam former is a spatially filtering which achieves this. If the restriction is  $g = 1$ , the message would be absorbed with the current gain inside the look position, and the reply will be distorted less. The Weighed Quantum Wolf Optimization (WQWO) beam former is a particular instance of the LCMV beam former, as seen in Figure 2.

A weight vector 'w' must be computed analytically for a restricted optimisation method.

$$(c * S_c)_c^{minimum} \quad (7)$$

$$c = \frac{S_z^{-1} x(\theta)}{a^H(\theta) S_z^{-1} x(\theta)} \quad (8)$$



**Fig. 2 WQWO-the optimum beam former pattern**

It is an optimal Weighed Quantum Wolf Optimization beam former. It displays the Wiener filter as

$$C = S^{-1} S \quad (9)$$

$$Weight\ of\ MVDR = \frac{(\sigma_{j,m})^{-1} x\theta}{x\theta^G (\sigma_{j,m})^{-1} x\theta} \quad (10)$$

$$r = Weight_{\theta} x\theta \quad (11)$$

Constructing existing covariance matrix training instances is a typical approach to calculating the correlation matrix.

$$S_{j,m} = \frac{1}{i} \sum_{i=1}^i a_{j,n(i)} a^G(i) \quad (12)$$

$i$ th training sample, and  $i$  is the total number.

While there are even minor arrays directing vector defects, the WQWO technique may experience considerable performance loss. Many methods for enhancing array guiding vector error resilience have been presented over the last few generations. A few of these techniques include vertical overloading, linear bounded minimal different beam forming, exponentially restricted beam forming, and second-order conical programmed. Customized colored diagonally loads are presented in this paper to enhance SINR and remove guiding vector mistakes.

**3.3. Diagonal Loading (DL)**

A tiny vertical matrix is introduced to the correlation matrix to address the abovementioned disadvantage. This method is known as vertical loaded or white noise stabilization. It can help distributed, and parallel beam formers withstand several circumstances, such as orientation incompatibility, component location, gain, phase incompatibility, and statistical incompatibility, owing to good statistical support. It is usually desired to find ways to

include vertical loads into beam forming techniques for its resilience. However, there is very little quantitative data about diagonal loads in the scientific literature.

Nevertheless, because of the non-stationary noise, the adaptable beam former can be trained with limited sample support. An optimum beam former's beam responsiveness may be defined concerning eigenvalues and eigenvectors. The eigenvalues are linear numbers that change based on the normal support 'k.' As a result, as the eigenvalues change, the beam responsiveness decreases. Consequently, the module that facilitates design has a greater side lobe intensity. Adding a balanced identity matrix to the sampling covariance matrix reduces the variance of the eigenvalues.

The reloading degree is added to those eigenvalues due to diagonally loading the covariance matrix. This causes a bias in such eigenvalues to reduce overall variance but causes a side bias in the adaptable weighting, lowering the resultant SINR. This noise power has to be equivalent to the minimal loading level. The variation of the generated white noise is increased by  $\sigma_L^2$  when a vertical load is used. This change requires the beam former to focus mostly on white noise suppression instead of interference reduction. Because the beam former puts lesser work into reducing disruptions & noise whenever the SOI guidance vectors are misaligned, the SOI is suppressed as one type of intervention. When  $\sigma_L^2$  is too big, though, the beam former is unable to reject and experiences extreme loss since it expends additional efforts suppressing white noise. As a result, there is a compromise between signal cancellations and effectual interfering suppression. As a result, selecting an appropriate vertical factor loading in the conventional WQWO beam former is difficult.

Figure 3 depicts a traditional vertical loaded beam former. That beam former may be viewed as a progressive transition between two distinct behaviors: completely adapted WQWO solutions ( $L = 0$ , no loads) and traditional uniform weighted beams patterns ( $L = \text{limitless loading}$ )

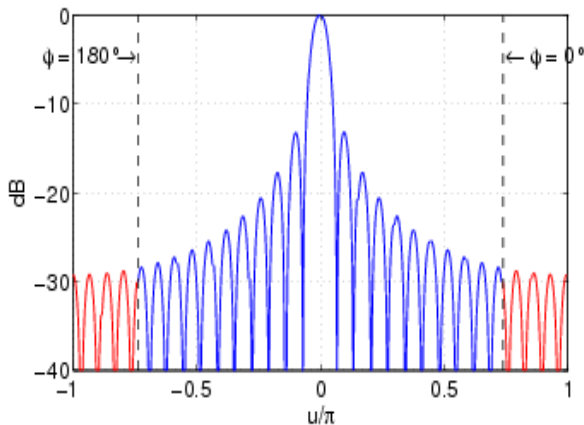


Fig. 3. Diagonal Loading (WQWO)

### 3.4. Colored Diagonal Loading (CDL)

It may be used in the absence of colored noises, and the warping procedure can culminate in a radiation pattern of our selection. The colored area is identical to WQWO DL, except it can change the diagonally loaded levels of the  $\sigma_L^2$  to the Infinity end state.

$$MVDR - CDL = [S - \sigma^2 K]x(\theta) \tag{13}$$

The correlation matrix reflects the intended quiet structure. That is calculated directly using either 1) a priori knowledge (e  $R_{dq}$  does not have to be vertical) or 2) the intended weighted vectors (in which  $R_{dq}$  must be diagonal). It is given, as

$$S = d([d(c_{dia})]^{-1}x(\theta)) \tag{14}$$

Where d is the intended quiescent weighted matrices. The colored vertical loaded shows no efficiency in pattern design, as shown in Figure 4.

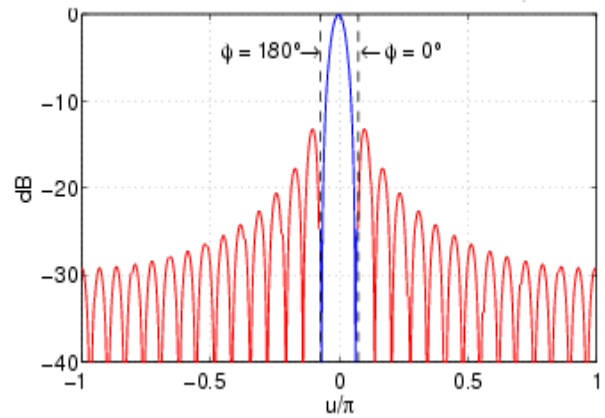


Fig. 4 Colored Diagonal Loading (WQWO)

### 3.5. Adaptive Diagonal Loading (ADL)

The preload amount is computed using this technique, which assumes that a priori knowledge about the SIGNAL TO NOISE is known and can be calculated by the network throughput or parameter estimation technique.

## 4. Computation

A 10 component Uniform Linear Arrays with Signal to the noise of 20 decibels for the intended signals received among  $\theta_s = 0^\circ$  and 72 decibels for 2 signals jammer originating from the direction  $\theta_i = -70^\circ$  and  $30^\circ$  is used in the suggested hybrid method. Several rays designs for beam forming algorithms are achieved compared to WQWO-ADL efficiency. The traditional beam formers behave well in obtaining optimum gain in the intended look orientation of  $0^\circ$ . However, it performs poorly when it comes to disturbance suppression.

The WQWO CDL technique works, and it outperforms the traditional beam former. It results in a higher SINR increase than the usual method. The blank is correctly positioned with no angle variation. The WQWO-ADL beam pattern is especially contrasted to other vertical loading techniques, which work to improve SINR. The beam morphologies of the methods mentioned above are shown in Figure 5. The fading channels' angles and the related beams' reactions are shown here.

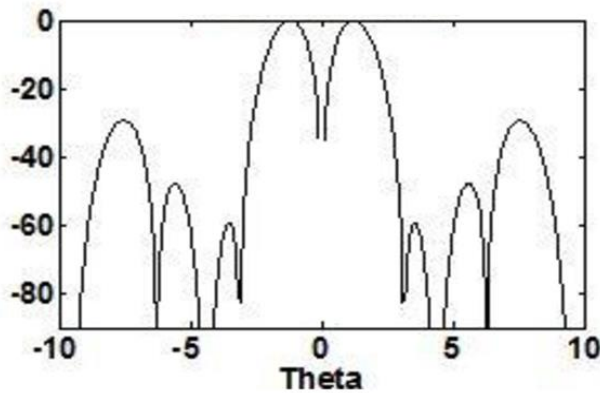


Fig. 5 Beam pattern WQWO-ACL. (a) Interferer 1 at angle -70°: -60 decibels. (b) Interferer 2 at angle 30°: -60 decibels

## 5. Results and Discussion

### 5.1. Number of Elements

The beam's designs were studied for the ULA, which would be regarded for experiments conducted by altering the number of components to 4, 8, 12, 16, 24, 50, and 100.

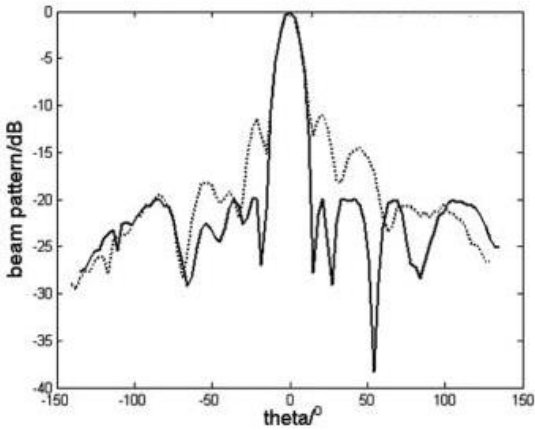


Fig. 6 Beam pattern of various diagonal loading methods

These technique works get significantly smaller as the number of components rises, i.e. the 3 decibels bandwidth narrows from 26° to 1° for traditional beam formers and 17° to 1° for adaptable diagonally loaded beam formers, as shown in Figure 6. Smaller or straighter rays are produced whenever a larger number of items are utilized. The narrower the beams, the less vulnerable the beam former is to jammers. However, the frequency of side lobes has grown as

well. Table 1 lists the 3-decibels beam width of several beam formers. It is possible to make a trade-off between cost and compactness. As a result, a max of 16 components is picked for further investigation. For studying the influence of disturbance on the peaks of the signal strength, a 16-element ULA is examined. Over 10 decibels to 60 decibels, the signal-to-noise ratio is changed into 10 decibels increments. The peak grows stronger as SIGNAL TO NOISE rises. It demonstrates that interruption generators are reduced to the greatest extent possible, ensuring that information extraction is not disrupted in the face of powerful multi-path.

Table 1. changing the number of antenna elements has an effect

Elements	Beamwidth						
	Complex	MVDR	SMI	Loading	DL in Color	Adapts	CDL Adapts
1	22	17.3	12.3	16	16	16	15
2	10.2	13.26	12.2	12.3	12.3	12.4	15.6
3	4.2	4.3	3.3	4.2	4.2	4.2	4.3
4	3.12	3.2	3.2	3.2	3.2	3.3	6.1
5	2.6	2.6	3	2.6	2.6	2.6	3.4

### 5.2. Element Spacing

For just a 16-component ULA, the separation here between components was adjusted as  $\lambda/4, \lambda/2, \lambda/3, \lambda/4$  and  $\lambda$  are modified to the array's overall apertures length. Among the 4 alternatives,  $\lambda/2$  performed the best for the specific frequency utilized in the experiments. Whenever the spacing between both the components was extended above  $\lambda/2$ , spatially interference occurred, resulting in many false peaks corresponding to various frequencies. These lasers' brightness wasn't adequate under  $\lambda/2$  shown in Figure 7.

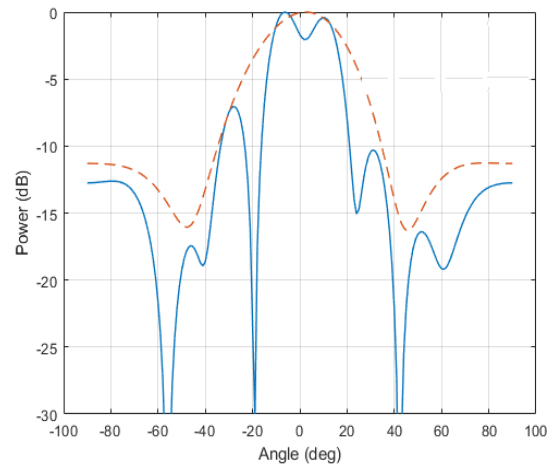


Fig. 7 Number of snapshots during training

Table 2 presents the comparisons and analytical conclusions of the responsiveness of several beamforming techniques.

**Table 2. Signals-desired beam response and jammers– comparison of multiple techniques**

Beam forming method	J = 1 Beam response power	J = 2 Beam response power	J = 2 Beam response power	J = 3 Beam response power
Conventional	1	-10	-10	-13
WQWO	1	-45	-33	-45
WQWO-SMI	1	-26	-30	-36
DL	1	-36	-37	-42
CDL	-3	-25	-26	-33
ADL	1	-26	-26	-43
ACDL	1	-26	-26	31

## 6. Conclusion

This research focuses on adaptable arrays beam forming inside the context of guiding vector mismatches and Sparsity impact issues. DL is one of the most commonly utilized strategies for coping with all these problems. The disadvantage of the diagonally loaded approaches is that it is unclear how to determine the appropriate diagonal loading level based on the recognized degree of uncertain restriction. Various DL techniques were subsequently presented for determining the necessary factor loadings, including the so-called automated system. This flaw is addressed in our study using a variable loading approach instead of constant diagonally loaded or Adhoc ways to incorporate the diagonal increasing dramatically into the adaptable updating system. The suggested WQWO technique is unique since it does not necessitate any complicated data strategy to determine the necessary loads. To address these problems, we implemented data-dependent reloading. The loaded component may be calculated entirely from the arrays of data provided. Analytic formulae for assessing the suggested product's performance in unpredictable guiding vector inaccuracy are indeed developed. Experimental findings demonstrate the suggested WQWO reliability compared to previous DL techniques.

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